

Useful Information

$$\mathbf{F}(d\mathbf{A}) = \boldsymbol{\Sigma} \, d\mathbf{A}$$

$$\epsilon_{ij} = \frac{1}{2} \left(\frac{\partial u_i}{\partial r_j} + \frac{\partial u_j}{\partial r_i} \right)$$

$$\mathbf{E} = \alpha e \mathbf{1} + \mathbf{E}'$$

$$\begin{aligned}\boldsymbol{\Sigma} &= \alpha e \mathbf{1} + \beta \mathbf{E}' \\ &= (\alpha - \beta) e \mathbf{1} + \beta \mathbf{E}\end{aligned}$$

$$\alpha = 3B_M \qquad \beta = 2S_M$$

$$e = \frac{1}{3}\,\mathrm{Tr}(\mathbf{E})$$

$$d\mathbf{u} = \mathbf{D} \, d\mathbf{r} \longrightarrow \mathbf{E} \, d\mathbf{r}$$

$$\rho \frac{\partial^2 \mathbf{u}}{\partial t^2} = \rho \mathbf{g} + \left(B_M + \frac{1}{3} S_M\right) \boldsymbol{\nabla} (\boldsymbol{\nabla} \cdot \mathbf{u}) + S_M \nabla^2 \mathbf{u}$$

$$\mathbf{F}_{\mathrm{inertial}} = \mathbf{F}_{\mathrm{fictitious}} = -m\mathbf{A}$$

$$\mathbf{v} = \boldsymbol{\omega} \times \mathbf{r}$$

$$\left(\frac{d\mathbf{Q}}{dt}\right)_{S_0} = \left(\frac{d\mathbf{Q}}{dt}\right)_S + \boldsymbol{\Omega} \times \mathbf{Q}$$

$$\mathbf{F}_{\mathrm{cor}} = 2m\dot{\mathbf{r}} \times \boldsymbol{\Omega} \quad \text{and} \quad \mathbf{F}_{\mathrm{cf}} = m(\boldsymbol{\Omega} \times \mathbf{r}) \times \boldsymbol{\Omega}$$

$$R_{\rm earth}=6.4\times10^6\,{\rm m}$$

$$\mathbf{R}=\frac{1}{M}\int\mathbf{r}\,dm$$

$$\mathbf{L}=\mathbf{L}(\text{motion of CM})+\mathbf{L}(\text{motion relative to CM})$$

$$T=T(\text{motion of CM})+T(\text{motion relative to CM})$$

$$\mathbf{L}=\mathbf{I}\boldsymbol{\omega}$$

$$I_{xx}=\sum_{\alpha}m_{\alpha}(y_{\alpha}^2+z_{\alpha}^2),\;\text{etc.}\;\;\text{and}\;\;\;I_{xy}=-\sum_{\alpha}m_{\alpha}x_{\alpha}y_{\alpha},\;\text{etc.}$$

$$\text{Principal Axis:}\quad \mathbf{L}=\lambda\boldsymbol{\omega}$$

$$\dot{\mathbf{L}}+\boldsymbol{\omega}\times\mathbf{L}=\boldsymbol{\Gamma}$$

$$T=\frac{1}{2}\sum_{j,k}M_{jk}\dot{q}_j\dot{q}_k\quad\text{and}\quad U=\frac{1}{2}\sum_{j,k}K_{jk}q_jq_k$$

$$(\mathbf{K}-\omega^2\mathbf{M})\mathbf{a}=0$$

$$\mathcal{L}=\mathcal{L}(q_i,\dot{q}_i,t)$$

$$\mathcal{L}=T-U$$

$$\frac{\partial \mathcal{L}}{\partial q_i} = \frac{d}{dt} \frac{\partial \mathcal{L}}{\partial \dot{q}_i}$$

$$p_i=\frac{\partial \mathcal{L}}{\partial \dot{q}_i}$$

$$\mathcal{H} = \sum_{i=1}^n p_i \dot{q}_i - \mathcal{L}$$

$$r(\phi) = \frac{c}{1+\epsilon\cos\phi}$$

$$E=\frac{\gamma^2\mu}{2\ell^2}(\epsilon^2-1)$$

$$\mathbf{r}=\mathbf{r}_1-\mathbf{r}_2\quad\text{and}\quad\mathbf{R}=\frac{m_1\mathbf{r}_1+m_2\mathbf{r}_2}{m_1+m_2}$$

$$\mu=\frac{m_1m_2}{m_1+m_2}$$

$$U_{\mathrm{eff}}=U(r)+\frac{\ell^2}{2\mu r^2}$$

$$\tau^2=\frac{4\pi^2}{GM}R^3$$

$$(\gamma_{n+1}-\gamma_n)\simeq \frac{1}{\delta}\left(\gamma_n-\gamma_{n-1}\right),\quad \text{where}\quad \delta=4.6692016\dots$$

$$f(x)=f(x_0)+(x-x_0)\left.\frac{df}{dx}\right|_{x=x_0}+\frac{1}{2}(x-x_0)^2\left.\frac{d^2f}{dx^2}\right|_{x=x_0}+\cdots$$

$$\mathbf{a}\cdot\mathbf{b}=a_ib_i$$

$$(\boldsymbol{\nabla} f)_i = \partial_i f$$

$$(\mathbf{a}\mathbf{\times}\mathbf{b})_i=\epsilon_{ijk}a_jb_k$$

$$\epsilon_{ijk}\epsilon_{ilm}=\delta_{jl}\delta_{km}-\delta_{jm}\delta_{kl}$$

$$\text{For tensor $\mathbf{M}$ and vector $\mathbf{a}$:}$$

$$(\mathbf{Ma})_i=M_{ij}a_j$$